

**16** Here are the first five terms of an arithmetic sequence.

7      10      13      16      19

Find the sum of the first 100 terms of this sequence.

.....  
(Total for Question 16 is 2 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**16** An arithmetic series has first term 1 and common difference 4

Find the sum of all terms of the series from the 41st term to the 100th term inclusive.

(Total for Question 16 is 4 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



- 18** In an arithmetic series, the 6th term is 39  
In the same arithmetic series, the 19th term is 7.8

Work out the sum of the first 25 terms of the arithmetic series.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 18 is 4 marks)



19 An arithmetic series has first term  $a$  and common difference  $d$

The sum of the first 30 terms of the arithmetic series is 4395

The sum of the 10th term and the 20th term is 284

Work out the sum of the first 45 terms of the arithmetic series.

Show clear algebraic working.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 19 is 5 marks)



- 19 The 25th term of an arithmetic series is 44.5  
The sum of the first 30 terms of this arithmetic series is 765

Find the 16th term of the arithmetic series.  
Show your working clearly.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 19 is 5 marks)



19 Here are the first 4 terms in an arithmetic sequence.

3      7      11      15

The last term of the sequence is  $x$

The sum of the terms of the sequence is 7260

Find the value of  $x$

Show clear algebraic working.

$x = \dots\dots\dots$

(Total for Question 19 is 6 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



20 The sum of the first 80 terms of an arithmetic series,  $S$ , is 470

The 75th term of  $S$  is 14.5

The sum of the first  $X$  terms of  $S$  is 171

Work out the value of  $X$

Show your working clearly.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

$X = \dots\dots\dots$

(Total for Question 20 is 6 marks)



20 Here are the first four terms of an arithmetic series.

$$k \quad \frac{3k}{4} \quad \frac{k}{2} \quad \frac{k}{4}$$

Given that the 15th term of the series is  $(90 + 2k)$ ,

calculate the sum of the first 30 terms of the series.

(Total for Question 20 is 5 marks)





- 21 The  $n$ th term of an arithmetic series is  $u_n$  where  $u_n > 0$  for all  $n$   
The sum to  $n$  terms of the series is  $S_n$

Given that  $u_4 = 6$  and that  $S_{11} = (u_6)^2 + 18$

find the value of  $u_{20}$

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 21 is 6 marks)



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- 22 The first term of an arithmetic series  $S$  is  $-6$   
The sum of the first 30 terms of  $S$  is 2865  
Find the 9th term of  $S$ .

(Total for Question 22 is 4 marks)



- 22 The first term of an arithmetic series is  $(2t + 1)$  where  $t > 0$   
The  $n$ th term of this arithmetic series is  $(14t - 5)$

The common difference of the series is 3

The sum of the first  $n$  terms of the series can be written as  $p(qt - 1)^r$  where  $p$ ,  $q$  and  $r$  are integers.

Find the value of  $p$ , the value of  $q$  and the value of  $r$   
Show clear algebraic working.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

$p = \dots\dots\dots$        $q = \dots\dots\dots$        $r = \dots\dots\dots$

(Total for Question 22 is 4 marks)



23 Here are the first three terms of an arithmetic sequence.

$$8p \qquad 7p - 3 \qquad 4p + 2$$

The sum of the first  $n$  terms of the sequence is  $-1914$

Work out the value of  $n$

Show your working clearly.

$$n = \dots\dots\dots$$

(Total for Question 23 is 5 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



- 23 A polygon has  $n$  sides, where  $n > 5$

When arranged in order of size, starting with the largest number, the sizes of the interior angles of the polygon, in degrees, are the terms of an arithmetic sequence.

Here are the first five terms of this sequence.

177      175      173      171      169

Find the value of  $n$

Show clear algebraic working.

$n = \dots\dots\dots$

(Total for Question 23 is 6 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

23 Work out the sum of the multiples of 3 between 1 and 1000

(Total for Question 23 is 4 marks)



- 23 The sum of the first  $N$  terms of an arithmetic series,  $S$ , is 292  
The 2nd term of  $S$  is 8.5  
The 5th term of  $S$  is 13

Find the value of  $N$ .

Show clear algebraic working.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

$N = \dots\dots\dots$

(Total for Question 23 is 5 marks)



- 23** The sum of the first 48 terms of an arithmetic series is 4 times the sum of the first 36 terms of the same series.

Find the sum of the first 30 terms of this series.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 23 is 5 marks)





23 Here are the first three terms of an arithmetic sequence.

$$(4x-14) \quad , \quad (x+2) \quad , \quad (7x-9)$$

Find, as an integer, the sum of the first 40 terms of the sequence.  
Show clear algebraic working.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 23 is 4 marks)



- 23 The 10th term of an arithmetic series,  $S$ , is 66  
The sum of the first 20 terms of  $S$  is 1290

Find the 5th term of  $S$ .  
Show your working clearly.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 23 is 4 marks)



24 A polygon has  $n$  sides, where  $n > 5$

The interior angles of the polygon form an arithmetic sequence.

The smallest angle of the polygon is  $84^\circ$

The common difference of the sequence is  $4^\circ$

Work out the sum of the interior angles of the polygon.

Show clear algebraic working.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 24 is 6 marks)



24 Here are the first five terms of an arithmetic sequence.

8      15      22      29      36

Work out the sum of all the terms from the 50th term to the 100th term inclusive.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 24 is 4 marks)



- 25 The sum of the first 10 terms of an arithmetic series is 4 times the sum of the first 5 terms of the same series.

The 8th term of this series is 45

Find the first term of this series.  
Show clear algebraic working.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 25 is 5 marks)



- 26 An arithmetic series has first term  $a$  and common difference  $d$ , where  $d$  is a prime number.

The sum of the first  $n$  terms of the series is  $S_n$  and

$$S_m = 39$$

$$S_{2m} = 320$$

Find the value of  $d$  and the value of  $m$

Show clear algebraic working.

$$d = \dots\dots\dots$$

$$m = \dots\dots\dots$$

(Total for Question 26 is 5 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



- 24 An arithmetic series has first term  $a$  and common difference  $d$ .

The sum of the first  $2n$  terms of the series is four times the sum of the first  $n$  terms of the series.

Find an expression for  $a$  in terms of  $d$ .  
Show your working clearly.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

 $a = \dots\dots\dots$ 

(Total for Question 24 is 4 marks)



- 24 An arithmetic sequence has first term 8 and common difference 11  
The sequence has  $k$  terms, where  $k > 21$

The sum of the last 20 terms of the sequence is 10 170

Find the value of  $k$

Show clear algebraic working.

$k = \dots\dots\dots$

(Total for Question 24 is 5 marks)





DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

25 Mario is going to save \$50 in the year 2021

He is going to continue to save, up to and including the year 2070, by increasing the amount he saves each year by \$ $k$

Mario will save a total of \$33 125 from 2021 to 2070

Work out the value of  $k$ .

$k = \dots\dots\dots$

(Total for Question 25 is 3 marks)

