

5 In the diagram below,  $P$  and  $Q$  are points on a circle with centre  $O$ .

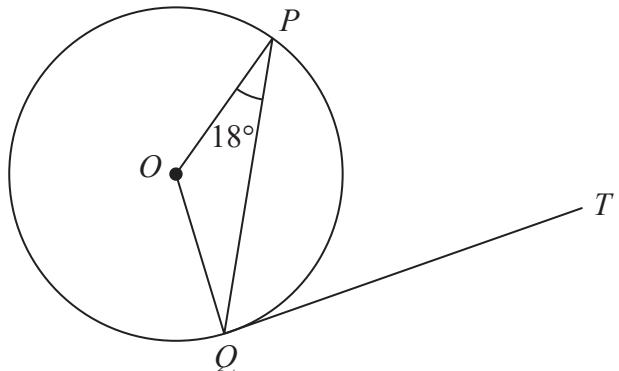


Diagram NOT  
accurately drawn

$QT$  is a tangent to the circle.

Angle  $OPQ = 18^\circ$

Work out the size of angle  $PQT$ .

Give a reason for each stage of your working.

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(Total for Question 5 is 3 marks)



7

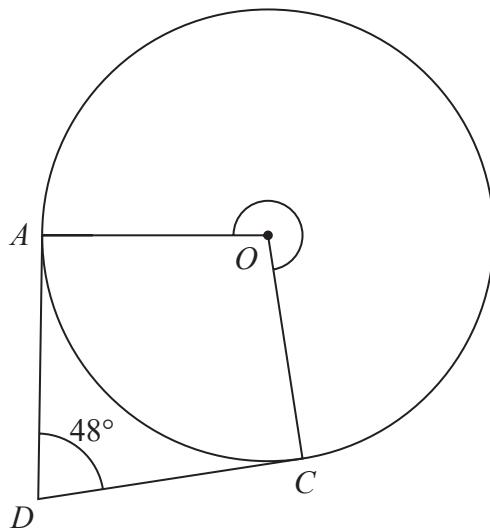


Diagram **NOT**  
accurately drawn

$A$  and  $C$  are points on a circle, centre  $O$

$DA$  is the tangent to the circle at  $A$  and  $DC$  is the tangent to the circle at  $C$

Angle  $ADC = 48^\circ$

Work out the size of reflex angle  $AOC$

(Total for Question 7 is 3 marks)

8



P 7 2 8 2 8 A 0 8 2 8



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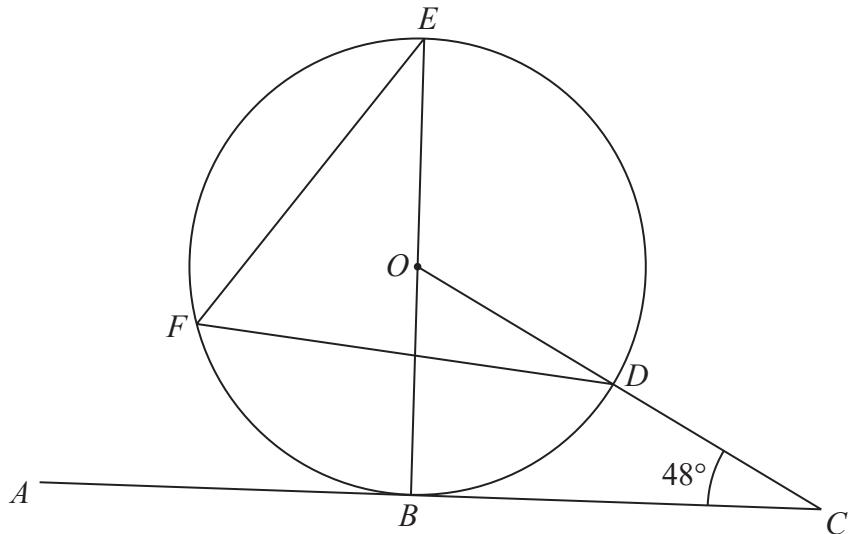


Diagram **NOT**  
accurately drawn

$B, D, E$  and  $F$  are points on a circle, centre  $O$ .

$ABC$  is a tangent to the circle.

$ODC$  is a straight line.

$BOE$  is a diameter of the circle.

$$\text{Angle } BCD = 48^\circ$$

Find the size of angle  $DFE$ .



12

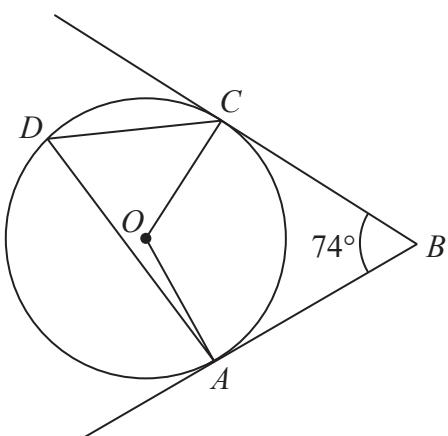


Diagram NOT  
accurately drawn

$A$ ,  $C$  and  $D$  are points on a circle, centre  $O$ .  
 $AB$  and  $CB$  are tangents to the circle.

Angle  $ABC = 74^\circ$

Work out the size of angle  $ADC$ .

Show your working clearly.

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(Total for Question 12 is 3 marks)



13

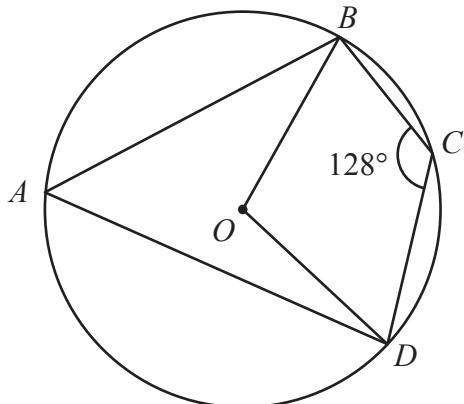


Diagram **NOT**  
accurately drawn

*A, B, C and D are points on a circle, centre O*

*Angle  $BCD = 128^\circ$*

*Work out the size of angle  $OBD$*

*Give a reason for each stage of your working.*

angle  $OBD = \dots^\circ$

**(Total for Question 13 is 5 marks)**

13

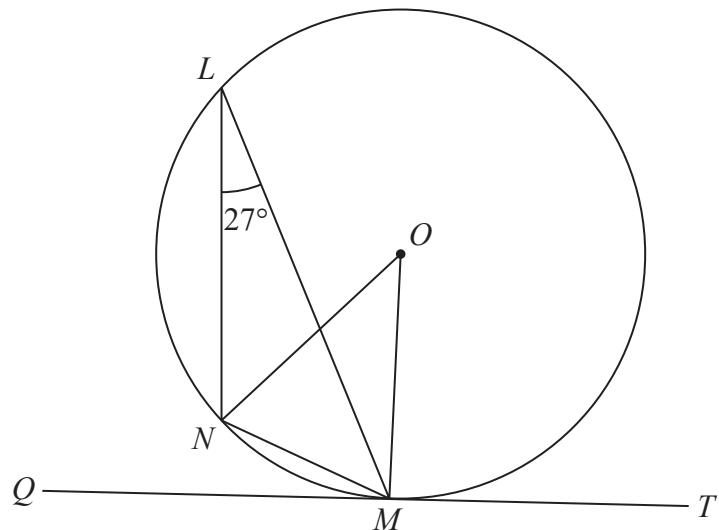


Diagram **NOT**  
accurately drawn

$L$ ,  $M$  and  $N$  are points on a circle, centre  $O$ .  
 $QMT$  is the tangent to the circle at  $M$ .

(a) (i) Find the size of angle  $NOM$ .

.....

(ii) Give a reason for your answer.

.....

(2)

(b) (i) Find the size of angle  $NMQ$ .

.....

(ii) Give a reason for your answer.

.....

(2)

**(Total for Question 13 is 4 marks)**



13  $P, Q, R, S$  and  $T$  are points on a circle with centre  $O$ .

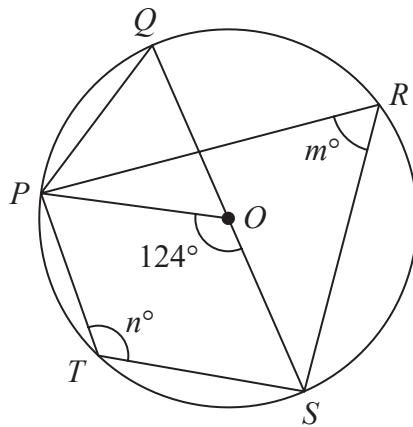


Diagram **NOT**  
accurately drawn

$QOS$  is a diameter of the circle.

$$\text{angle } POS = 124^\circ \quad \text{angle } PRS = m^\circ \quad \text{angle } PTS = n^\circ$$

(a) Find the value of

(i)  $m$

(ii)  $n$

.....  
(2)

(b) Find the size of angle  $QPO$ .

.....  
(1)

**(Total for Question 13 is 3 marks)**

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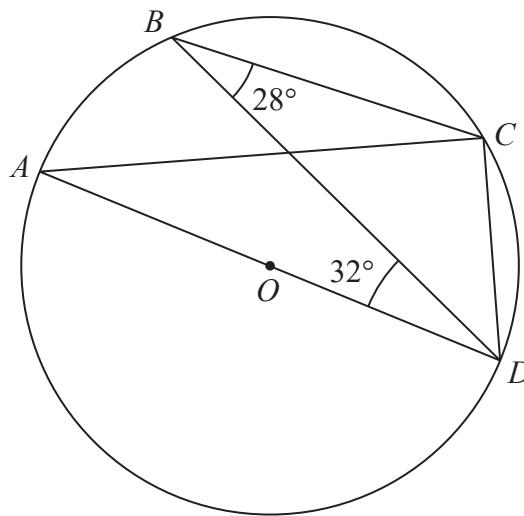
**13**

Diagram **NOT**  
accurately drawn

*A, B, C and D are points on a circle, centre O.  
AOD is a diameter of the circle.*

Angle  $CBD = 28^\circ$

Angle  $BDA = 32^\circ$

Find the size of angle  $BDC$ .

Give a reason for each stage of your working.

**(Total for Question 13 is 4 marks)**



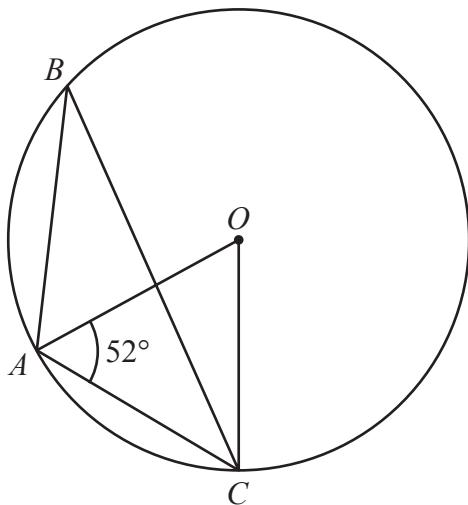
**14**

Diagram **NOT**  
accurately drawn

*A, B and C are points on a circle, centre O*

*Angle  $OAC = 52^\circ$*

*Find the size of angle  $ABC$*

*Give reasons for your working.*

**(Total for Question 14 is 3 marks)**

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**14**  $A$ ,  $B$  and  $C$  are points on a circle, centre  $O$

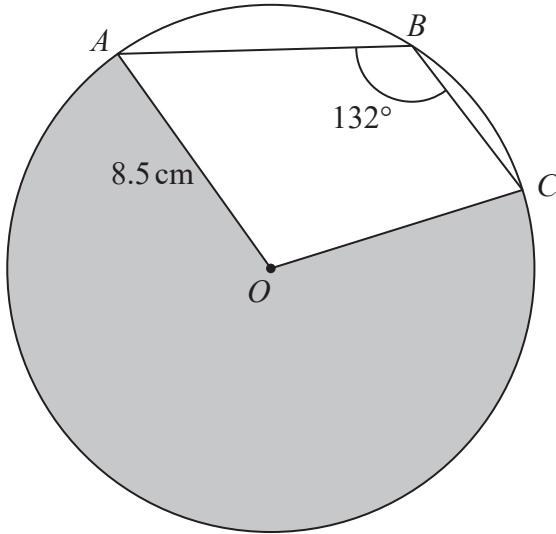


Diagram **NOT**  
accurately drawn

The radius of the circle is 8.5 cm

Angle  $ABC = 132^\circ$

Work out the perimeter of the shaded sector  $AOC$

Give your answer correct to 3 significant figures.

..... cm

**(Total for Question 14 is 3 marks)**



P 7 2 4 4 4 A 0 1 5 3 2

14

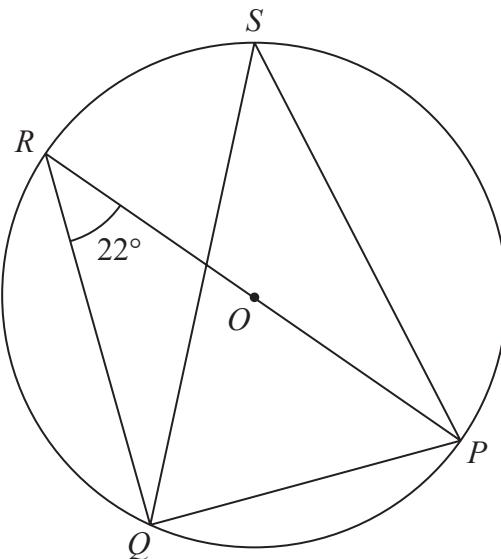


Diagram **NOT**  
accurately drawn

$P, Q, R$  and  $S$  are points on a circle, centre  $O$

*ROP* is a diameter of the circle.

Angle  $PRQ = 22^\circ$

(a) (i) Find the size of angle  $RQP$

(1)

(ii) Give a reason for your answer.

(1)

(b) (i) Find the size of angle  $PSQ$

(1)

(ii) Give a reason for your answer.

(1)

**(Total for Question 14 is 4 marks)**



14  $A, B, C$  and  $D$  are points on a circle, centre  $O$

$EBF$  is the tangent to the circle at  $B$

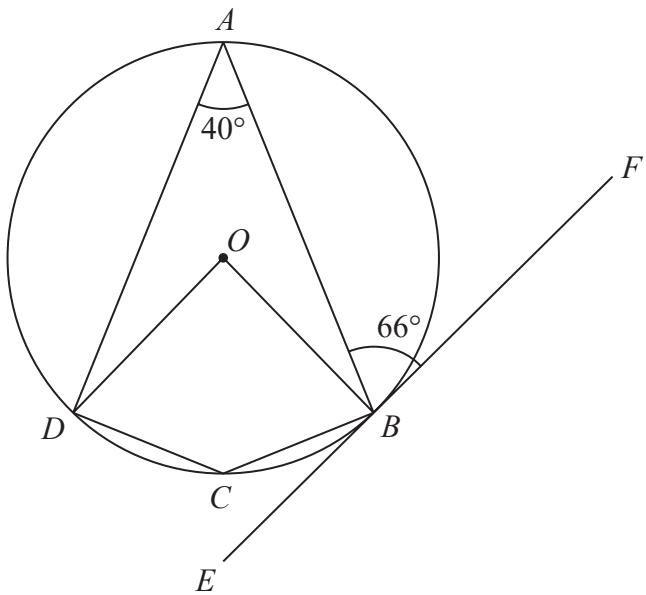


Diagram **NOT**  
accurately drawn

(a) (i) Work out the size of angle  $DCB$

.....  
.....  
.....  
.....  
(1)

(ii) Give a reason for your answer to (a)(i)

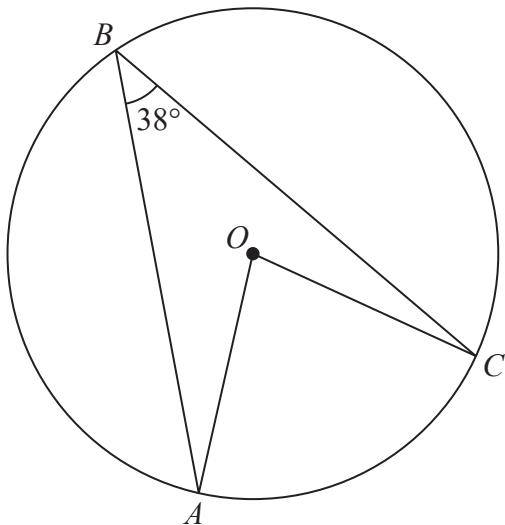
.....  
.....  
.....  
.....  
(1)

(b) Work out the size of angle  $ADO$

.....  
.....  
.....  
.....  
(3)

**(Total for Question 14 is 5 marks)**



**14****Diagram NOT  
accurately drawn**

$A, B$  and  $C$  are points on a circle, centre  $O$ .

Angle  $ABC = 38^\circ$

Work out the size of angle  $OAC$ .

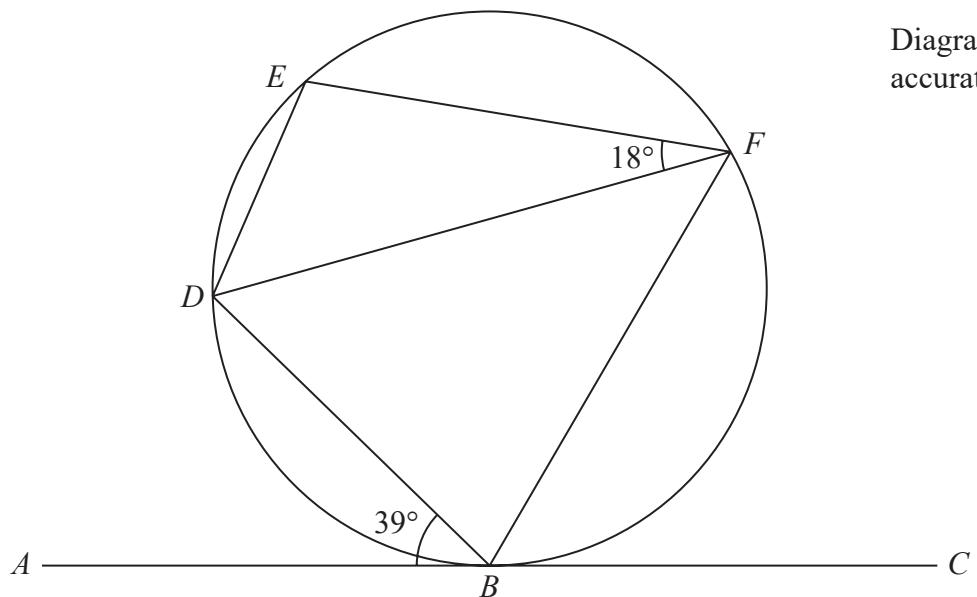
Give a reason for each stage of your working.

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.....

**(Total for Question 14 is 4 marks)**

P 5 8 4 4 3 A 0 1 4 2 4

**14**

$B, D, E$  and  $F$  are points on a circle.

$ABC$  is the tangent at  $B$  to the circle.

Angle  $ABD = 39^\circ$

Angle  $EFD = 18^\circ$

Work out the size of angle  $BDE$ .

Give reasons for your working.

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(Total for Question 14 is 4 marks)



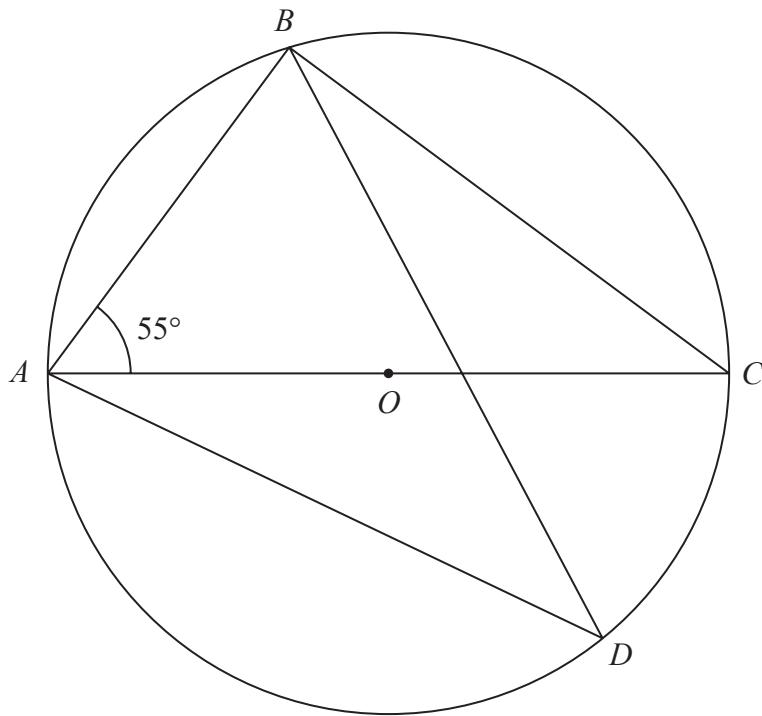
**14**

Diagram NOT  
accurately drawn

*A, B, C and D are points on a circle, centre O  
AOC is a diameter of the circle.*

Angle  $BAC = 55^\circ$

Work out the size of angle  $ADB$   
Give a reason for each stage of your working.

(Total for Question 14 is 4 marks)



15  $A, B, C$  and  $D$  are points on a circle, centre  $O$ .

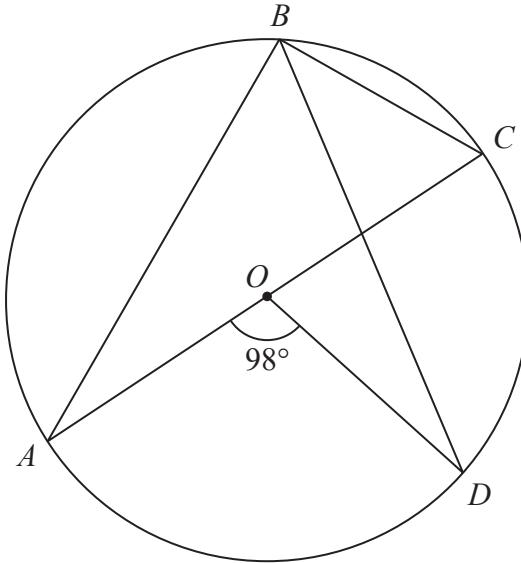


Diagram NOT  
accurately drawn

$AOC$  is a diameter of the circle.

Angle  $AOD = 98^\circ$

Work out the size of angle  $DBC$ .

Give a reason for each stage in your working.

(Total for Question 15 is 4 marks)



P 6 0 2 6 1 A 0 1 3 2 4

15

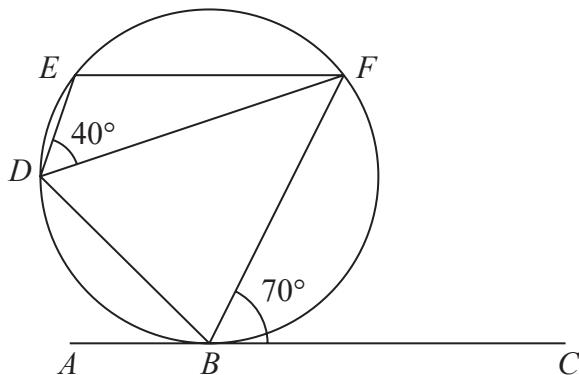


Diagram NOT  
accurately drawn

$B, D, E$  and  $F$  are points on a circle.  
 $ABC$  is the tangent to the circle at  $B$ .

Angle  $EDF = 40^\circ$   
Angle  $FBC = 70^\circ$

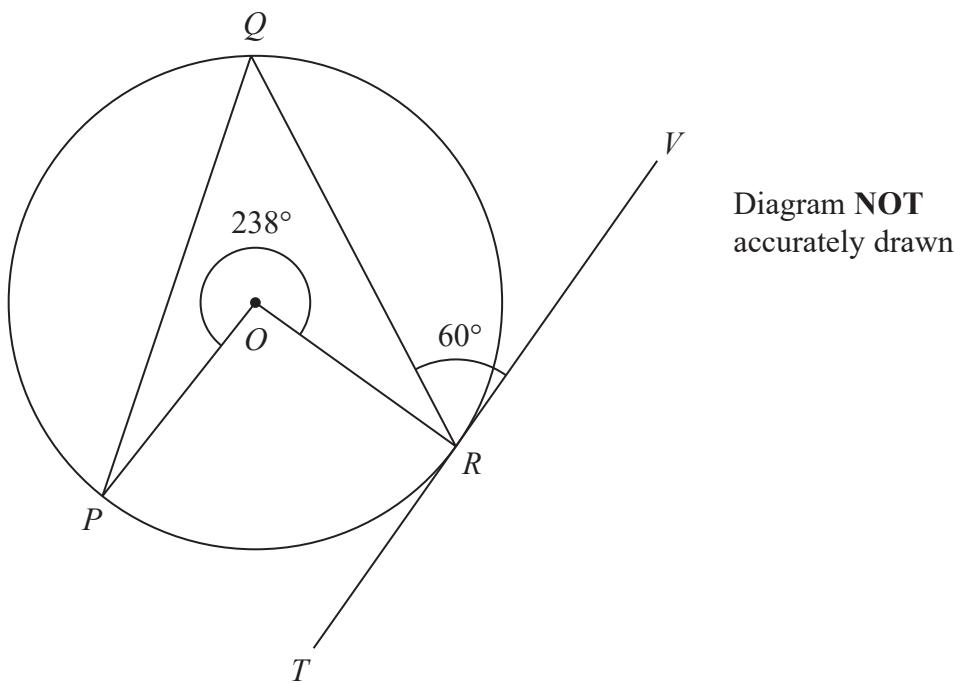
Prove that the tangent  $ABC$  is parallel to  $EF$ .  
Give a reason for each stage of your working.

(Total for Question 15 is 4 marks)



P 6 2 6 5 3 A 0 1 5 2 4

15  $P$ ,  $Q$  and  $R$  are points on a circle, centre  $O$ .  
 $TRV$  is the tangent to the circle at  $R$ .



Reflex angle  $POR = 238^\circ$

Angle  $QRV = 60^\circ$

Calculate the size of angle  $OPQ$ .

Give a reason for each stage of your working.

(Total for Question 15 is 4 marks)



15

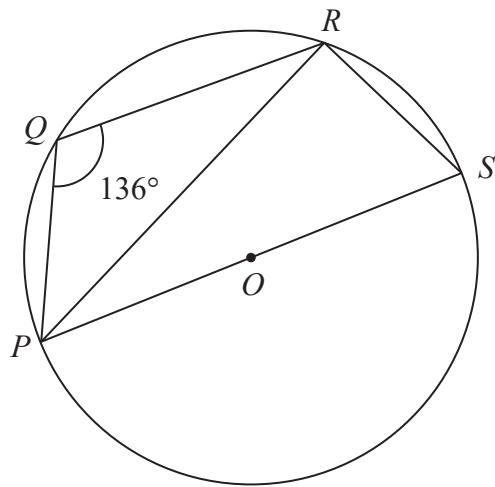


Diagram NOT  
accurately drawn

$P, Q, R$  and  $S$  are points on a circle with centre  $O$

$PS$  is a diameter of the circle.

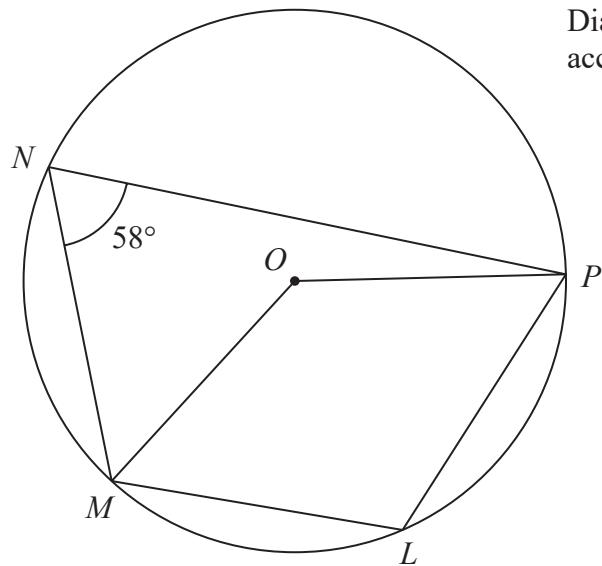
Angle  $PQR = 136^\circ$

Work out the size of angle  $RPS$

(Total for Question 15 is 3 marks)



P 6 8 7 8 9 A 0 1 7 2 8

**16****Diagram NOT  
accurately drawn**

$L, M, N$  and  $P$  are points on a circle, centre  $O$

Angle  $MNP = 58^\circ$

(a) (i) Find the size of angle  $MLP$

.....  
.....

(ii) Give a reason for your answer.

.....  
.....  
.....  
.....

(2)

(b) Find the size of the reflex angle  $MOP$

.....  
.....  
.....  
.....

(2)

**(Total for Question 16 is 4 marks)**



16  $A, B, C$  and  $D$  are points on a circle, centre  $O$

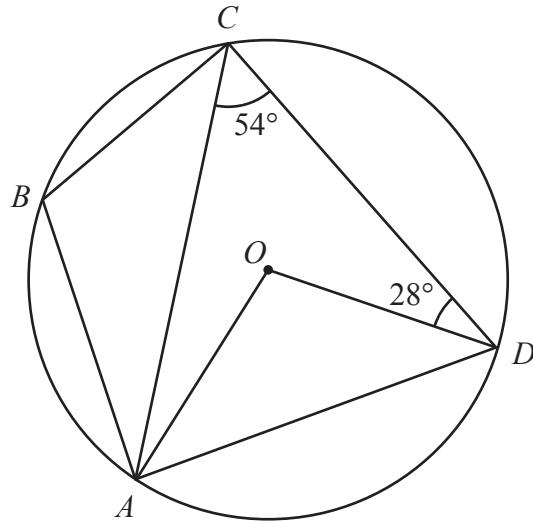


Diagram **NOT**  
accurately drawn

(a) (i) Work out the size of angle  $AOD$

(1)

(ii) Give a reason for your answer to part (a)(i)

(1)

(b) Work out the size of angle  $CAO$

(1)

(c) Work out the size of angle  $ABC$

(2)

**(Total for Question 16 is 5 marks)**



16  $D, E, F$  and  $G$  are points on a circle, centre  $O$

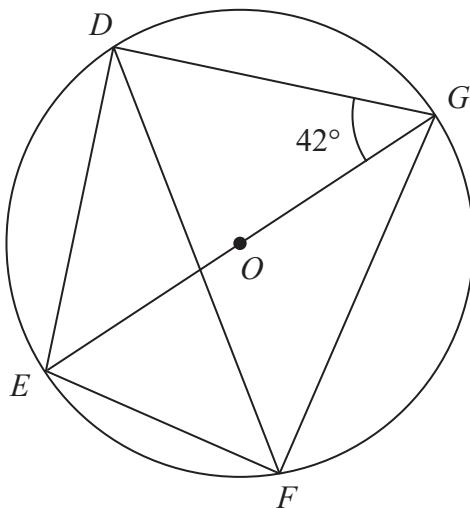


Diagram NOT  
accurately drawn

$EOG$  is a diameter of the circle.

Angle  $EGD = 42^\circ$

Calculate the size of angle  $DFG$

Give a reason for each stage of your working.

Angle  $DFG = \dots$   $^\circ$

**(Total for Question 16 is 4 marks)**



16

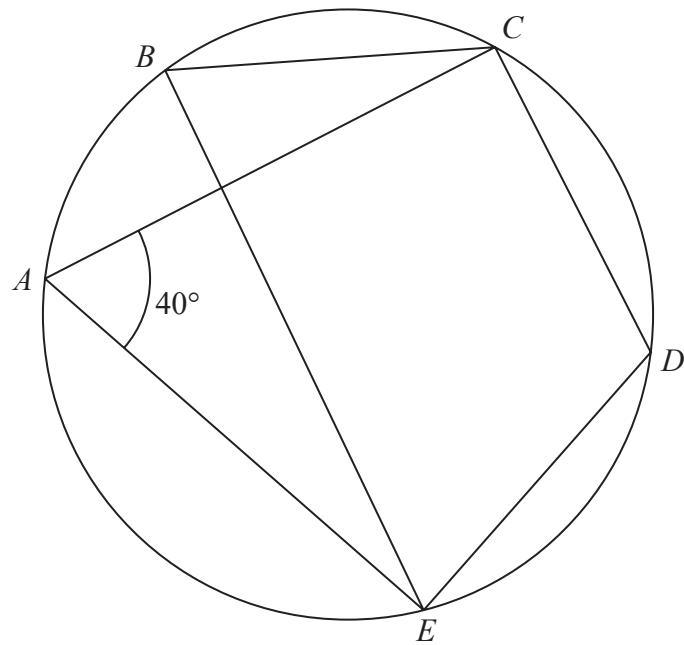


Diagram **NOT**  
accurately drawn

$A, B, C, D$  and  $E$  are points on a circle.

$\text{Angle } EAC = 40^\circ$

(a) (i) Write down the size of angle  $EBC$ .

.....  
.....  
(1)

(ii) Give a reason for your answer.

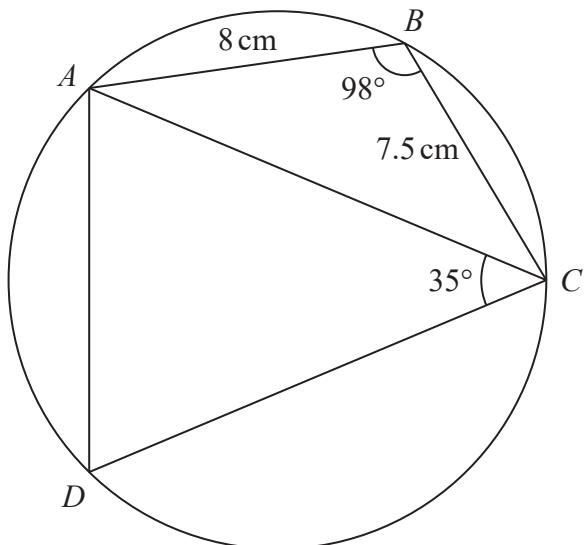
.....  
.....  
(1)

(b) Find the size of angle  $EDC$ .

.....  
.....  
(1)

**(Total for Question 16 is 3 marks)**



**18****Diagram NOT  
accurately drawn**

*ABCD* is a quadrilateral where *A*, *B*, *C* and *D* are points on a circle.

$$AB = 8 \text{ cm}$$

$$BC = 7.5 \text{ cm}$$

$$\text{Angle } ABC = 98^\circ$$

$$\text{Angle } ACD = 35^\circ$$

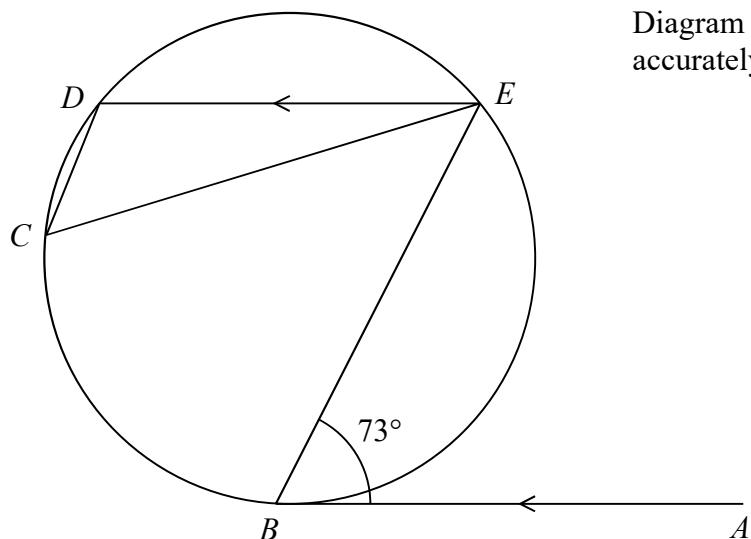
Work out the perimeter of quadrilateral *ABCD*.

Give your answer correct to one decimal place.

..... cm

**(Total for Question 18 is 6 marks)**

19



$B, C, D$  and  $E$  are points on a circle.

$AB$  is the tangent at  $B$  to the circle.

$AB$  is parallel to  $ED$ .

Angle  $ABE = 73^\circ$

Work out the size of angle  $DCE$ .

Give a reason for each stage of your working.

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(Total for Question 19 is 5 marks)



19

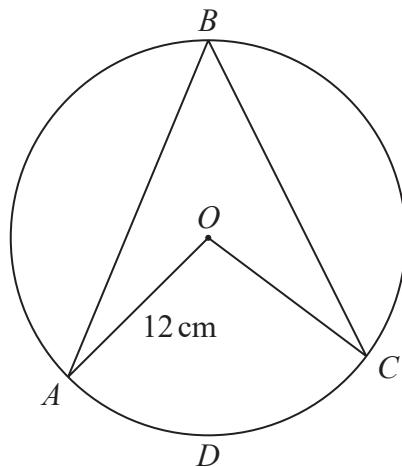


Diagram **NOT**  
accurately drawn

$A, B, C$  and  $D$  are points on a circle with centre  $O$  and radius 12 cm.

The area of the sector  $OADC$  of the circle is  $100 \text{ cm}^2$

Work out the size of angle  $ABC$ .

Give your answer correct to 3 significant figures.

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(Total for Question 19 is 4 marks)



20  $A$ ,  $B$  and  $C$  are points on a circle.

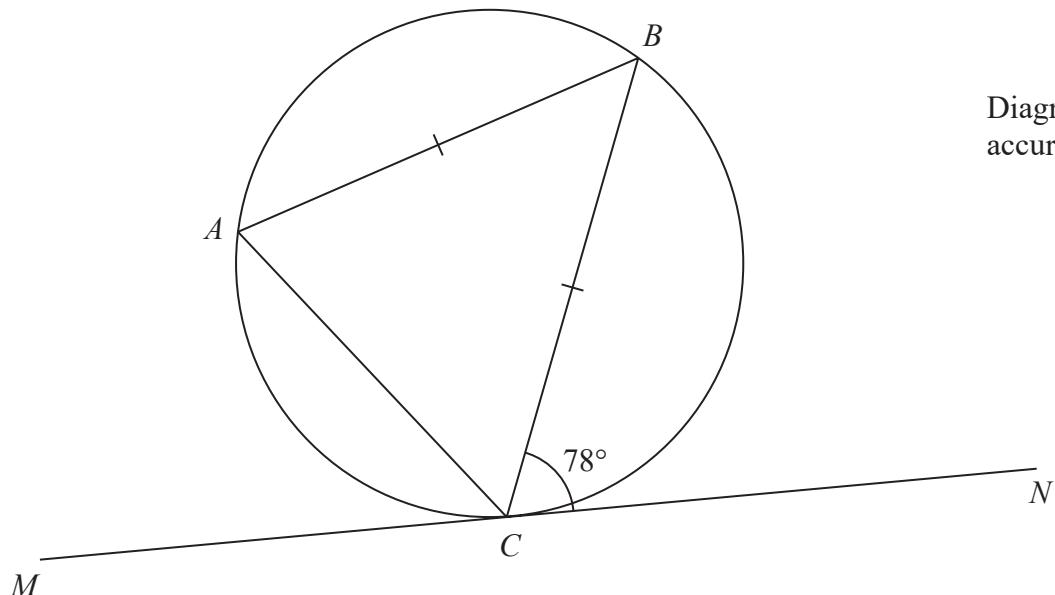


Diagram NOT  
accurately drawn

$MN$  is the tangent to the circle at  $C$

$$AB = CB$$

$$\text{Angle } BCN = 78^\circ$$

Find the size of angle  $ABC$

(Total for Question 20 is 2 marks)



20

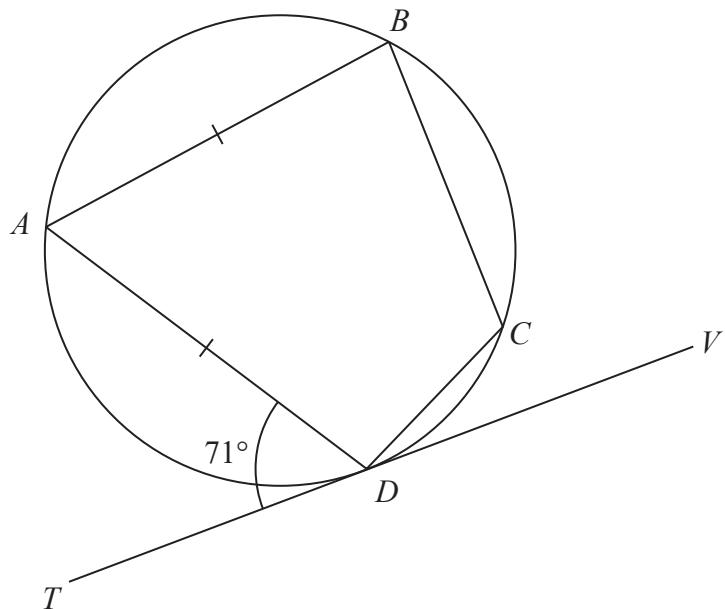


Diagram **NOT**  
accurately drawn

$A, B, C$  and  $D$  are points on a circle.  
 $TDV$  is the tangent to the circle at  $D$ .

$$AB = AD$$

Angle  $ADT = 71^\circ$

Work out the size of angle  $BCD$ .  
Give a reason for each stage of your working.

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(Total for Question 20 is 5 marks)



20

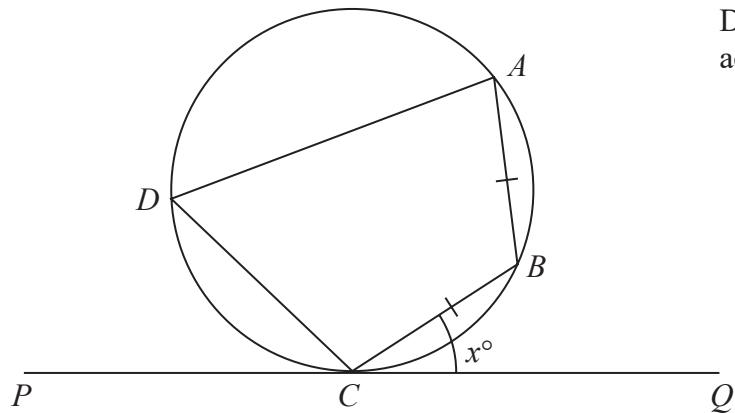


Diagram **NOT**  
accurately drawn

$A, B, C$  and  $D$  are points on a circle.  
 $PCQ$  is a tangent to the circle.  
 $AB = CB$ .

Angle  $BCQ = x^\circ$

Prove that angle  $CDA = 2x^\circ$

Give reasons for each stage in your working.

(Total for Question 20 is 5 marks)



P 5 9 0 1 9 A 0 2 1 2 4

20  $A$ ,  $B$  and  $C$  are points on a circle with centre  $O$ .

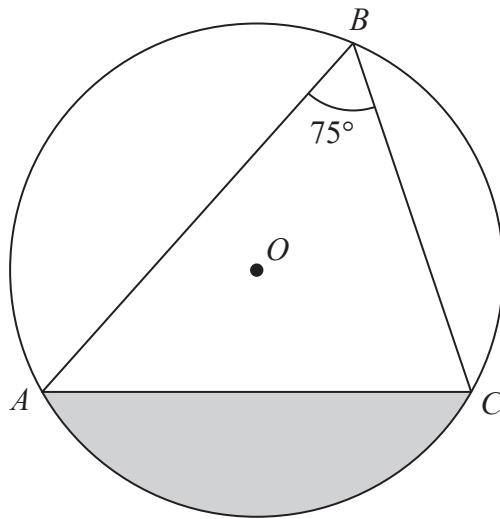


Diagram NOT  
accurately drawn

Angle  $ABC = 75^\circ$

The area of the shaded segment is  $200 \text{ cm}^2$

Calculate the radius of the circle.

Give your answer correct to 3 significant figures.

..... cm

(Total for Question 20 is 5 marks)



P 6 6 3 0 2 A 0 1 9 2 4

23

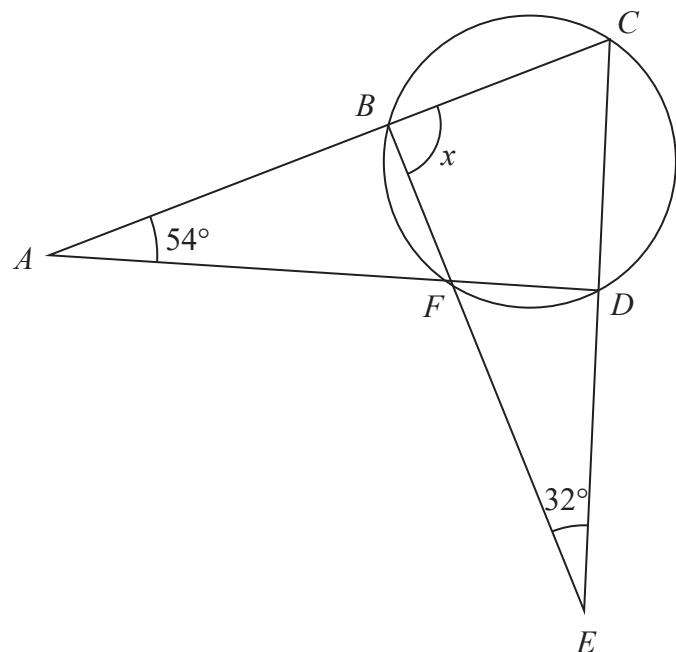


Diagram **NOT**  
accurately drawn

$B, C, D$  and  $F$  are points on a circle.  
 $ABC, AFD, BFE$  and  $CDE$  are straight lines.

Work out the size of angle  $x$ .  
Show your working clearly.

$$x = \dots \text{ } ^\circ$$

(Total for Question 23 is 4 marks)

